Mixed QCD × EW $\mathcal{O}(\alpha\alpha_s)$ corrections to Drell–Yan processes in the resonance region

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– in collaboration with Alexander Huss and Christian Schwinn –

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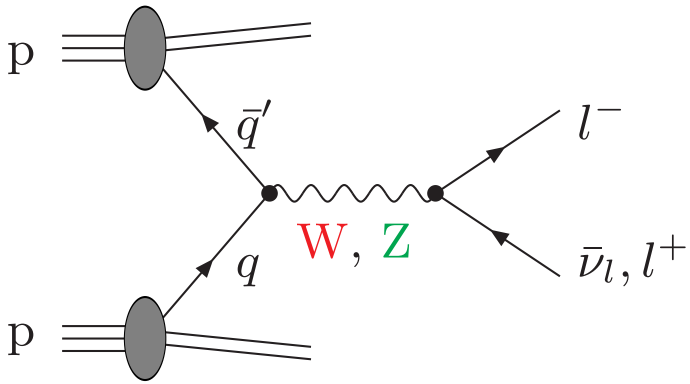
Introduction

—

corrections to Drell–Yan processes

W- and Z-boson production at hadron colliders



Physics issues:

- σ $\rightarrow$ standard candle
- M_Z $\rightarrow$ detector calibration by comparing with LEP1 result
- $\sin^2\theta_{\mathrm{eff}}^{\mathrm{lept}}$ $\rightarrow$ comparison with results of LEP1 and SLC
- M_W $\rightarrow$ improvement over $\Delta M_W \sim 15\,\mathrm{MeV}$, strengthen EW precision tests (W/Z shape comparisons even sensitive to $\Delta M_W \sim 7\,\mathrm{MeV}$ at LHC)
  Besson et al. '08
- decay widths Γ_Z and Γ_W from M_{ll} or $M_{T,l\nu_l}$ tails
- search for Z' and W' at high M_{ll} or $M_{T,l\nu_l}$
- information on PDFs

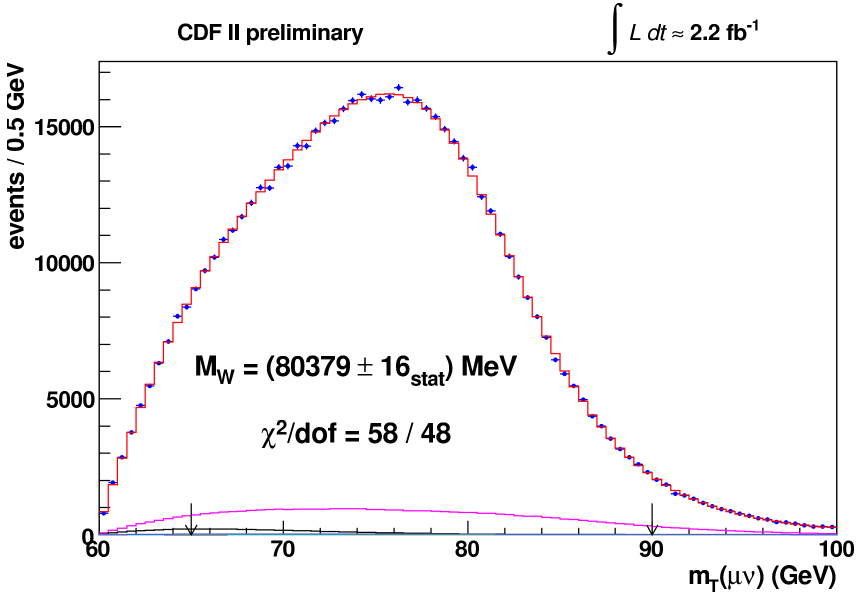
Tevatron example: M_{W} determination @ CDF (2012)

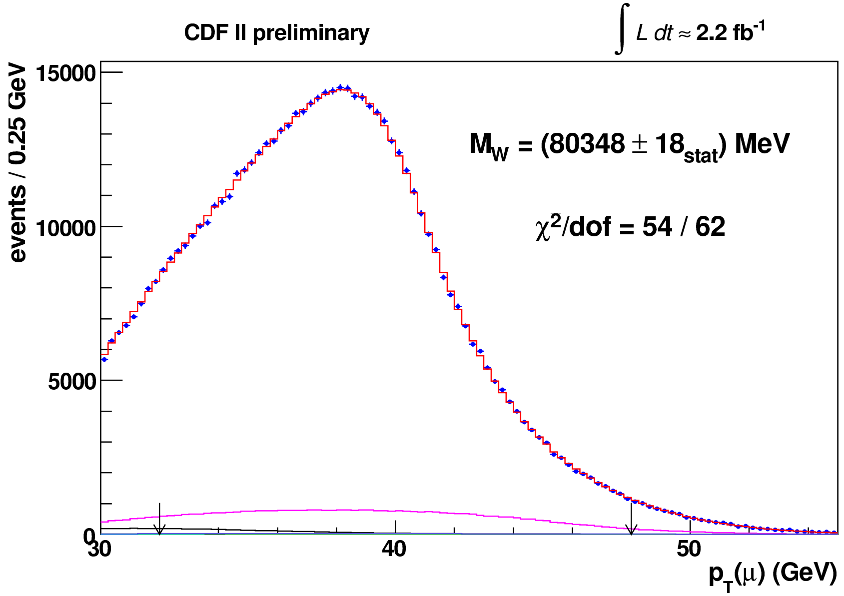
$M_{\mathrm{W}}^{\mathrm{CDF}} = 80.387\,\mathrm{GeV} \pm 19\,\mathrm{MeV}$ from fits to distributions in

a) transverse W-boson mass

$$M_{\mathrm{T},l\nu} = \sqrt{2(E_{\mathrm{T},l}\not{E}_{\mathrm{T}} - \mathbf{p}_{\mathrm{T},l}\cdot \not{\mathbf{p}}_{\mathrm{T}})}$$

b) transverse lepton momentum $p_{\mathrm{T},l}$





Sensitivity to M_{W} via Jacobian peaks from W resonance at

$$M_{\mathrm{T},l\nu} \sim M_{\mathrm{W}} \qquad\qquad p_{\mathrm{T},l} \sim M_{\mathrm{W}}/2$$

$\Rightarrow$ Reduction of ΔM_{W} requires higher theoretical precision in W resonance region !

(for Z resonance as well for reference)

Combination of NLO QCD and EW corrections

Issue unambiguously fixed only by calculating the 2-loop $\mathcal{O}(\alpha\alpha_s)$ corrections, until then rely on approximations and estimate the uncertainties:

Comparison of two extreme alternatives:

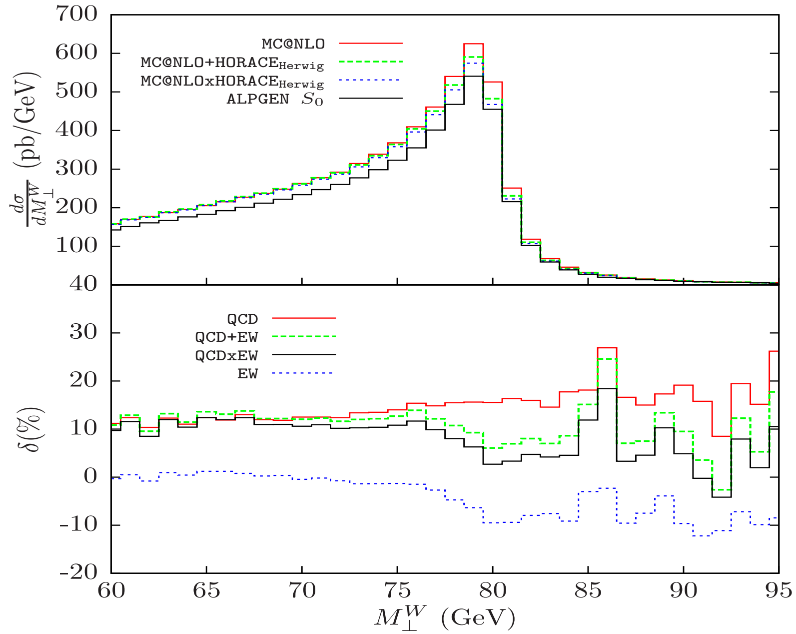
$$(1+\delta_{\rm QCD}^{\rm NLO}+\delta_{\rm EW}^{\rm NLO})$$

versus

$$(1+\delta_{\rm QCD}^{\rm NLO})\times(1+\delta_{\rm EW}^{\rm NLO})$$

$\hookrightarrow$ difference at %-level with shape distortion

Balossini et al. '09 (HORACE)



$\Rightarrow$ $\mathcal{O}(\alpha\alpha_s)$ corrections should be known at least in resonance region !

QCD and EW corrections to W/Z production:

NNLO QCD + NLO EW

+ QCD resummations / parton-shower matching

+ improvements known

Steps towards $\mathcal{O}(\alpha\alpha_s)$ corrections

- NLO EW for W/Z production with a hard jet
  - $\mathrm{W}/\mathrm{Z}/\gamma + 1\,\mathrm{jet}$, stable W/Z bosons — Maina, Moretti, Ross '04; Kühn, Kulesza, Pozzorini, Schulze '04–'07; Hollik, Kasprzik, Kniehl '07; Hollik, Kniehl, Shcherbakova, Veretin '15
  - off-shell W/Z bosons with decays — Denner, S.D., Kasprzik, Mück '09–'12

    $\mathrm{W} + 1\,\mathrm{jet} \to l\nu_l + 1\,\mathrm{jet}, \qquad \mathrm{Z}/\gamma^* + 1\,\mathrm{jet} \to l^+l^-/\bar{\nu}_l\nu_l + 1\,\mathrm{jet}$
- further partial results
  - on-shell $\mathrm{Z}f\bar{f}$ vertex — Kotikov, Kühn, Veretin '07
  - virtual corrections to $q\bar{q}' \to \mathrm{W}/\mathrm{Z} \to l\bar{l}'$ — Bonciani '11; Kilgore, Sturm '11
  - inclusive $\Gamma_{\mathrm{W}\to q\bar{q}'}$ — Kara '13
- resonance expansion for $q\bar{q}' \to \mathrm{W}/\mathrm{Z} \to l\bar{l}'$ — S.D., Huss, Schwinn '13–'15

This talk
+ A.Huss in
Mo parallel III

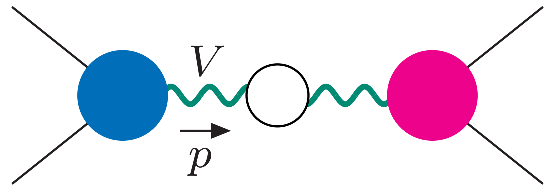
Pole expansion @ $\mathcal{O}(\alpha)$

Pole expansion of loop amplitudes – general idea

Stuart '91; H.Veltman '92
Aeppli, v.Oldenborgh, Wyler '94

Starting point: Dyson-summed matrix element

$$\mathcal{M} = \underbrace{\frac{W(p^2)}{p^2 - M_V^2 + \Sigma(p^2)}} + N(p^2)$$



resonant part with complex pole at $p^2 = \mu_V^2 = M_V^2 - \mathrm{i} M_V \Gamma_V$ gauge invariant

Sirlin '91; Stuart '91; Gambino, Grassi '99; Grassi, Kniehl, Sirlin '01

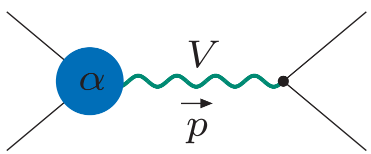
$$= \underbrace{\frac{W(\mu_V^2)}{p^2 - \mu_V^2} \frac{1}{1 + \Sigma'(\mu_V^2)}} + \underbrace{\left[\frac{W(p^2)}{p^2 - M_V^2 + \Sigma(p^2)} - \frac{W(\mu_V^2)}{p^2 - \mu_V^2} \frac{1}{1 + \Sigma'(\mu_V^2)} \right] + N(p^2)}$$

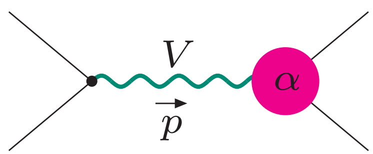
resonance pole = gauge invariant
$\hookrightarrow$ "factorizable contributions"

resonant "non-factorizable" corrections
$+$ non-resonant continuum

Virtual factorizable corrections

$$\mathcal{M}_{\text{fact}}^{(1)} = \sum_\lambda \frac{\mathcal{M}_{\text{production}}^{(1)}(\lambda) \mathcal{M}_{\text{decay}}^{(0)}(\lambda) + \mathcal{M}_{\text{production}}^{(0)}(\lambda) \mathcal{M}_{\text{decay}}^{(1)}(\lambda)}{p^2 - \mu_V^2}$$





Comments:

respect V-spin correlations; $W(\mu_V^2) \to W(M_V^2)$ possible in $\mathcal{O}(\alpha)$ and $\mathcal{O}(\alpha_s \alpha)$

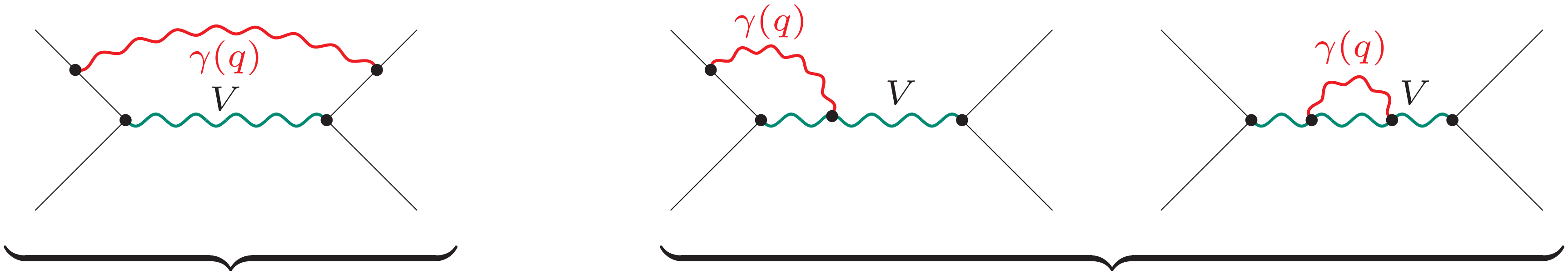
Virtual non-factorizable corrections

Fadin, Khoze, Martin ’94; Melnikov, Yakovlev ’96; Beenakker, Berends, Chapovsky ’97; Denner, Dittmaier, Roth ’97,’98

Origin:

on-shell limit ($p^2 \to M_V^2$) and IR regularization (e.g. $m_\gamma \to 0$) do not commute

for γ exchange between external and/or resonant lines:



“manifestly non-factorizable”

- resonant IR-divergent contribution

“not manifestly non-factorizable” diagrams

- fact. contribution: $W(M_V^2)$
- non-factorizable part:
  $W_{\mathrm{non-fact}}(p^2) \equiv \left[W(p^2) - W(M_V^2)\right]_{p^2 \to M_V^2}$

General features:

Fadin, Khoze, Martin ’94

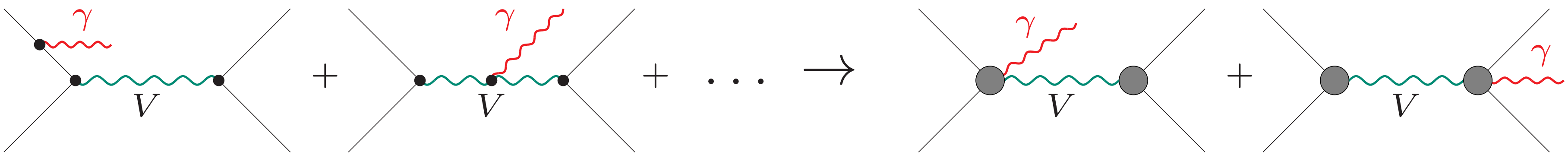
- contributions only from soft momenta $|q^\mu| \sim \Gamma_V \ll M_V$
  $\hookrightarrow$ calculation within “extended soft-photon approximation” (keep off-shell V propagators)
- result factorizes from Born amplitude: $\mathcal{M}^{\mathrm{virt}}_{\mathrm{non-fact}} = \delta^{\mathrm{virt}}_{\mathrm{non-fact}}\, \mathcal{M}^{(0)}$
- virtual + real non-fact. corrections cancel in inclusive quantities such as σ_{tot}

Pole expansion of real photonic corrections

Split diagrams with radiating resonances (2 resonant propagators) as follows:

$$\frac{1}{[(p+k)^2-\mu_V^2](p^2-\mu_V^2)} = \frac{1}{2pk}\left[\frac{1}{p^2-\mu_V^2} - \frac{1}{(p+k)^2-\mu_V^2}\right]$$

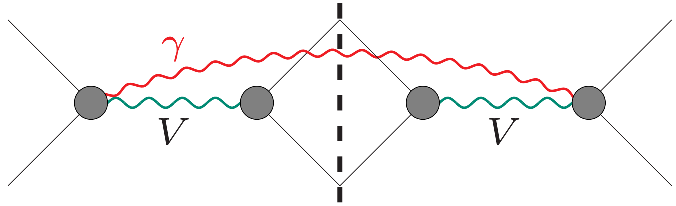
$\hookrightarrow$ decomposition of $\mathcal{M}_{i\to f+\gamma}$ into initial- and final-state radiation:



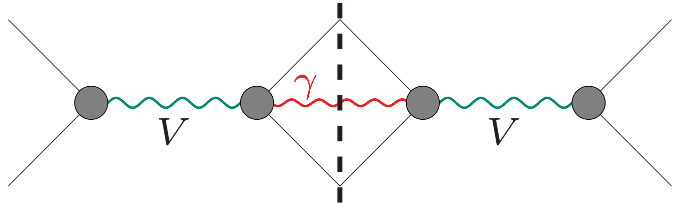
● = on-shell tree-like subamplitudes

Classification of real photonic corrections in PA

Factorizable contributions to $|\mathcal{M}|^2$:

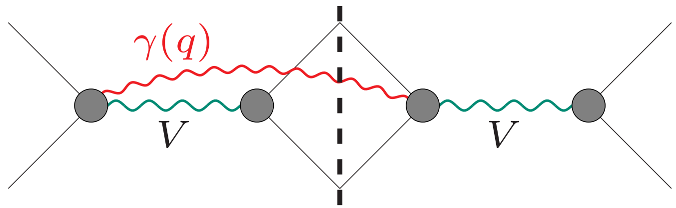


Initial-state radiation



Final-state radiation

Non-factorizable contributions to $|\mathcal{M}|^2$:



$+$ c.c.

Only $q = \mathcal{O}(\Gamma_V)$ relevant !

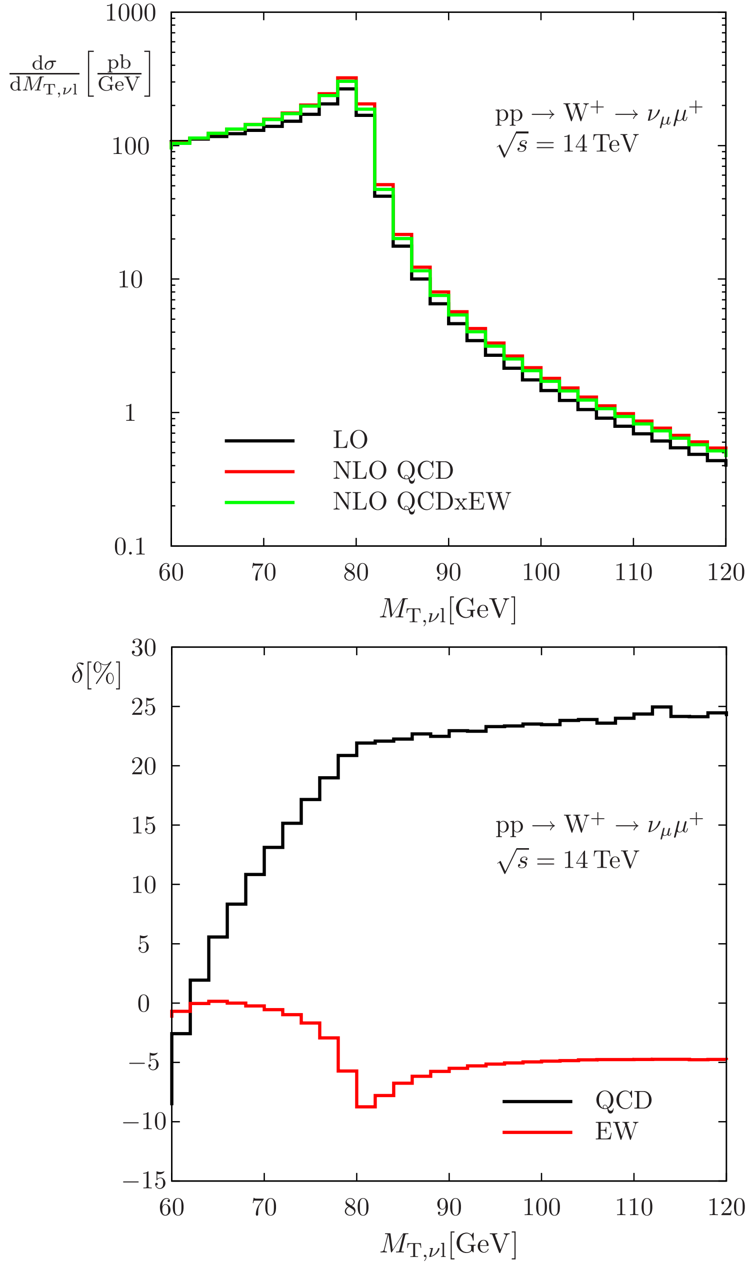
calculable from modified eikonal currents:

$$\mathrm{d}\sigma_{\mathrm{non-fact}} = \mathrm{d}\sigma_0\, \delta^{\mathrm{real}}_{\mathrm{non-fact}}, \qquad \delta^{\mathrm{real}}_{\mathrm{non-fact}} = \frac{\alpha}{2\pi^2}\int \frac{\mathrm{d}^3\mathbf{q}}{q^0}\, \mathrm{Re}\{\mathcal{J}^\mu_{\mathrm{prod}}\mathcal{J}^*_{\mathrm{dec},\mu}\},$$

$$\mathcal{J}^\mu_{\mathrm{prod}} = Q_1\frac{p_1^\mu}{p_1 q} - Q_2\frac{p_2^\mu}{p_2 q} - (Q_1 - Q_2)\frac{(p_1+p_2)^\mu}{p_1 q + p_2 q},$$

$$\mathcal{J}^\mu_{\mathrm{dec}} = \left[-Q'_1\frac{k_1^\mu}{k_1 q} + Q'_2\frac{k_2^\mu}{k_2 q} + (Q'_1 - Q'_2)\frac{(k_1+k_2)^\mu}{k_1 q + k_2 q}\right]\frac{(k_1+k_2)^2-\mu_V^2}{(k_1+k_2+q)^2-\mu_V^2}$$

Transverse-mass distribution for W production



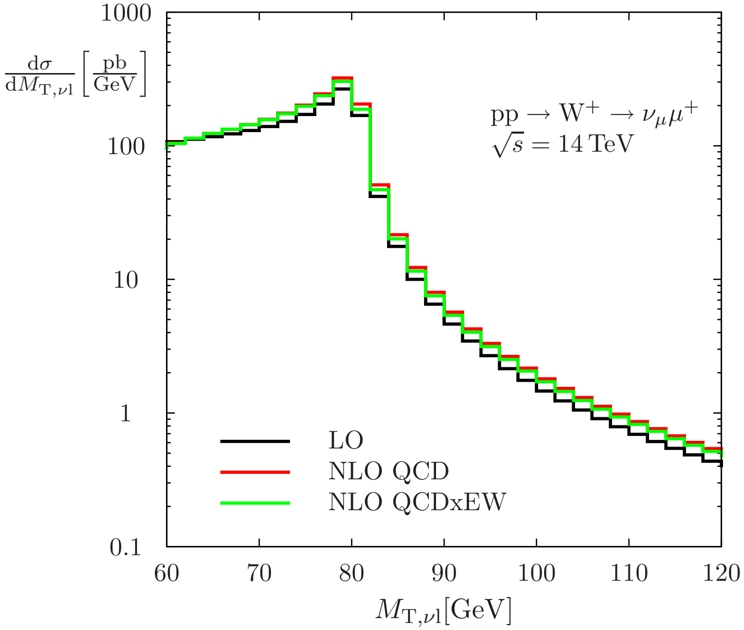
Features of $M_{\mathrm{T},\nu l}$:

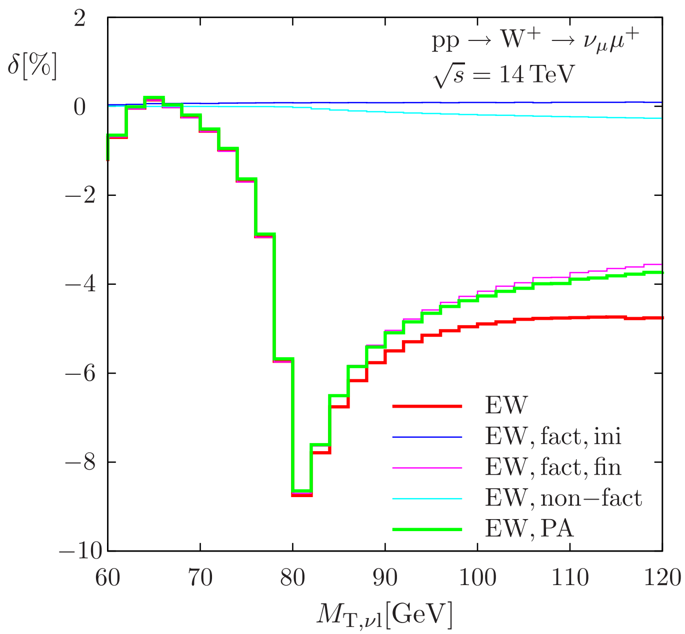
- most important observable for M_{W} det.
- stability wrt QCD corrs/uncertainties (insensitive to jet recoil)
- sensitive to detector effects via $\not{E}_{\mathrm{T}}$

Corrections:

- QCD corrections quite flat near resonance
- EW corrections distort resonance shape

Transverse-mass distribution for W production





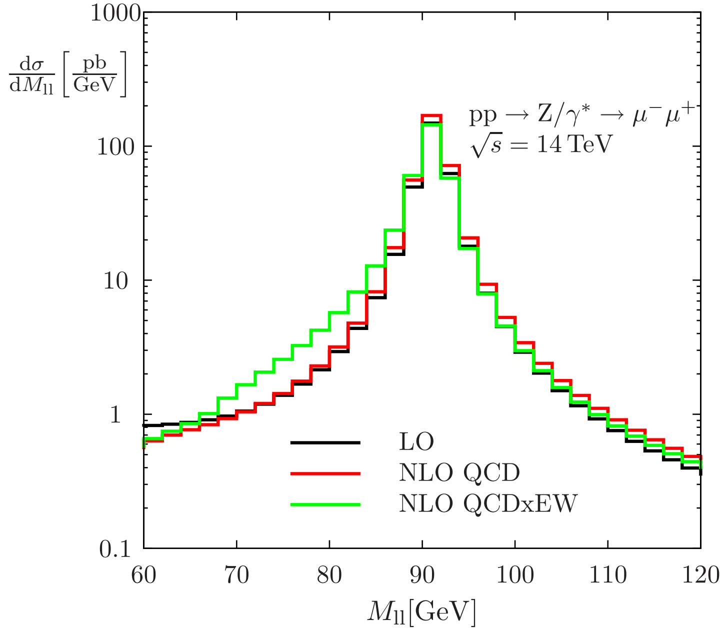
Features of $M_{T,\nu l}$:

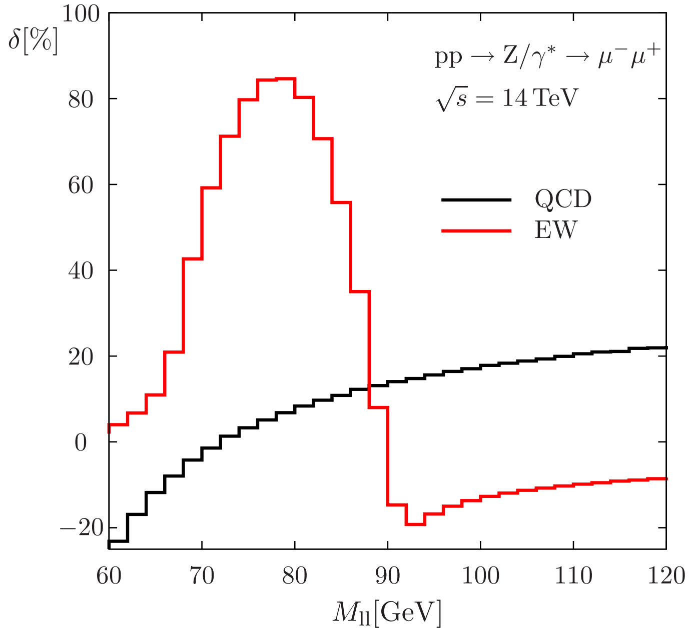
- most important observable for M_W det.
- stability wrt QCD corrs/uncertainties (insensitive to jet recoil)
- sensitive to detector effects via $\not{E}_T$

Pole approximation (PA):

- PA reproduces EW corr near resonance
- resonance distortion merely due to factorizable FS correction
- factorizable IS and non-fact. corrections flat (and even negligible)

Invariant-mass distribution for Z production



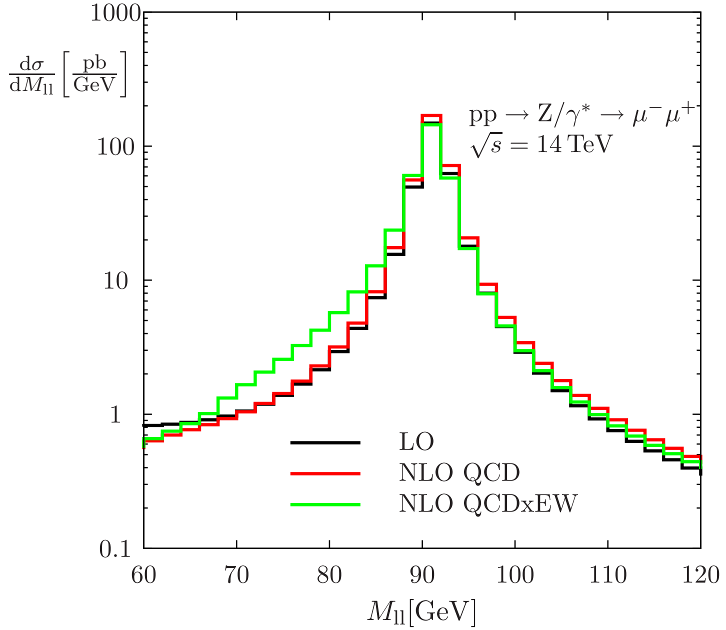


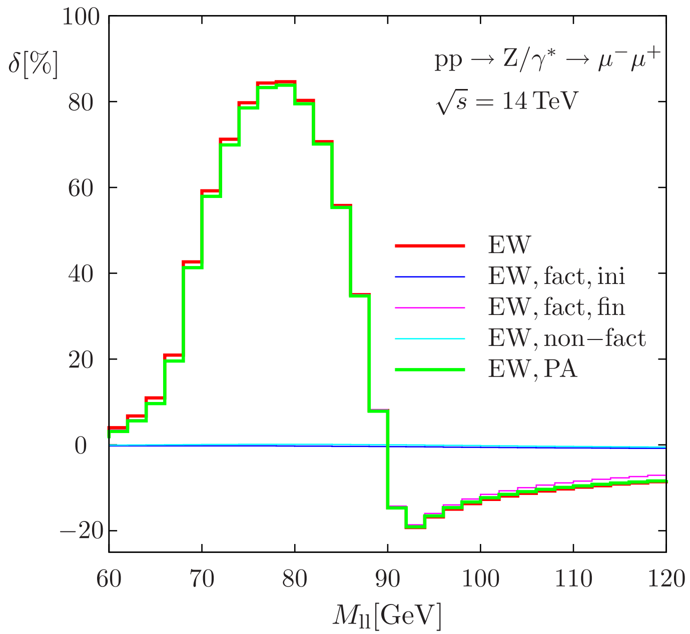
Reference process for M_W measurement

Corrections:

- QCD corrections quite flat near resonance
- EW corrections distort resonance shape

Invariant-mass distribution for Z production





Reference process for M_W measurement

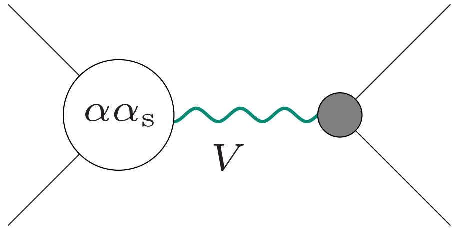
Behaviour of PA analogous to $M_{T,\nu l}$:

- PA reproduces EW corr near resonance
- resonance distortion merely due to factorizable FS correction
- factorizable IS and non-fact. corrections flat (and even negligible)

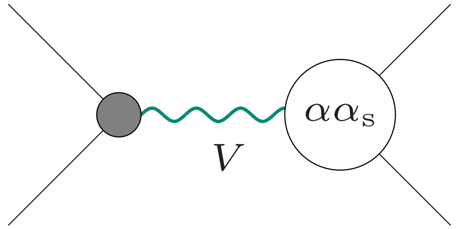
Pole expansion @ $\mathcal{O}(\alpha\alpha_{\rm s})$
and
non-factorizable corrections

Classification of $\mathcal{O}(\alpha\alpha_s)$ corrections in PA

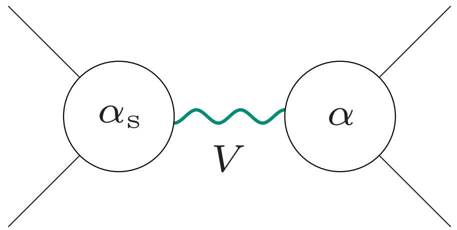
Factorizable contributions: (only virtual contributions indicated)



- no significant resonance distortion expected
- no PDFs with $\mathcal{O}(\alpha\alpha_s)$ corrections

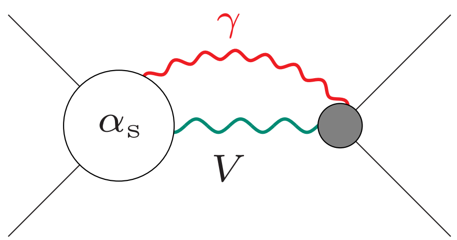


- only $Vl\bar{l}'$ counterterm contributions
  $\hookrightarrow$ uniform rescaling, no distortions



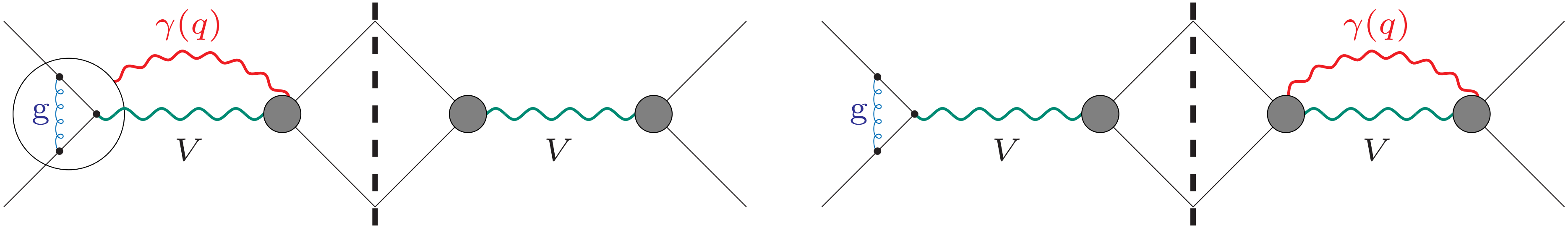
- significant resonance distortions from FSR

Non-factorizable contributions: (only virtual contributions indicated)



- small @ $\mathcal{O}(\alpha)$, but could be enhanced by large $\mathcal{O}(\alpha_s)$ corrections (jet recoil)

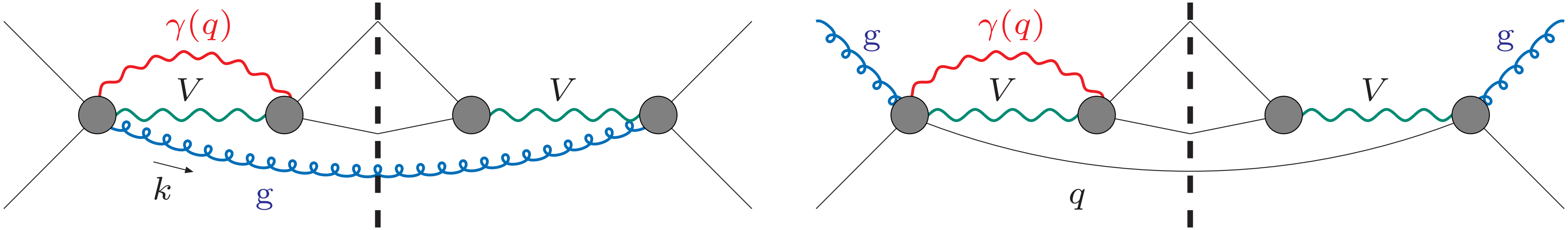
Virtual–virtual contributions to non-factorizable $\mathcal{O}(\alpha\alpha_s)$ corrections



Result: $$|\mathcal{M}|^2\Big|_{\substack{\text{non-fact}\\ \text{virt-virt}}} = 4\,\mathrm{Re}\{\delta^{(\alpha_s,\text{virt})}_{q\bar{q}'V}\}\,\mathrm{Re}\{\delta^{(\alpha,\text{virt})}_{\text{non-fact}}\}\,|\mathcal{M}_0|^2$$

- factorized structure (1-loop) $\times$ (1-loop) after non-trivial cancellations
- expansion of all loops in $q^\mu \sim \Gamma_V \sim (p^2-\mu_V^2)/M_V \to 0$
- issue of overlapping IR singularities
- different methods applied $\to$ results agree
  - ◇ diagrammatic calculation (expansion via Mellin–Barnes technique)
  - ◇ gauge-invariance argument à la Yennie/Frauschti/Suura '61 (even holds to any order $\alpha\alpha_s^n$, $n=1,2,\ldots$)
  - ◇ effective field theory for unstable particles Beneke et al. '03,'04

Virtual–real contributions to non-factorizable $\mathcal{O}(\alpha\alpha_s)$ corrections



Result: $$\left.|\mathcal{M}|^2\right|_{\substack{\mathrm{non-fact}\\ \mathrm{virt-real}}} = 2\,\mathrm{Re}\{\delta^{(\alpha,\mathrm{virt})}_{\mathrm{non-fact},q\bar{q}'\to l\bar{l}'\mathrm{g}}\}\,|\mathcal{M}_{0,q\bar{q}\to l\bar{l}'\mathrm{g}}|^2,$$ etc.

- From explicit diagrammatic calculation analogous to NLO $\mathcal{O}(\alpha)$ calculation
- New feature in qg channels: γ exchange between final-state particles
  Structure different from initial–final interferences $\rightarrow$ enhancement ?

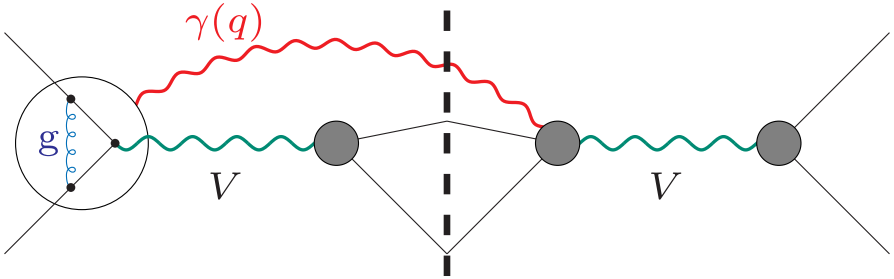
Example: W production $u\bar{d} \to \mathrm{W} \to \nu_l l^+ \mathrm{g}$

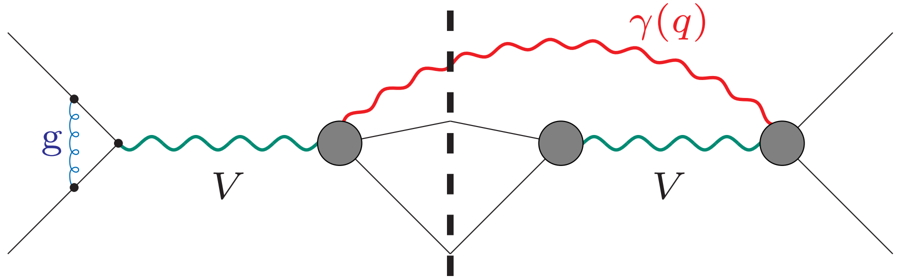
$$\delta^{(\alpha,\mathrm{virt})}_{\mathrm{non-fact},u\bar{d}\to\nu_l l^+\mathrm{g}} = -\frac{\alpha}{2\pi}\Biggl\{-2 + Q_d\,\mathrm{Li}\left(1+\frac{M_\mathrm{W}^2-\hat{t}_{u\mathrm{g}}}{\hat{t}_{dl}}\right) - Q_u\,\mathrm{Li}\left(1+\frac{M_\mathrm{W}^2-\hat{t}_{d\mathrm{g}}}{\hat{t}_{ul}}\right)$$
$$-\left[\frac{c_\epsilon}{\epsilon} - 2\ln\left(\frac{\mu_\mathrm{W}^2-\hat{s}}{\mu M_\mathrm{W}}\right)\right]\left[1 + Q_d\ln\left(\frac{M_\mathrm{W}^2-\hat{t}_{u\mathrm{g}}}{-\hat{t}_{dl}}\right) - Q_u\ln\left(\frac{M_\mathrm{W}^2-\hat{t}_{d\mathrm{g}}}{-\hat{t}_{ul}}\right)\right]\Biggr\}$$

($\hat{t}_{qj} = (p_q - k_j)^2$, on-shell projection for W !)

$$\xrightarrow[k\to 0]{} \quad \delta^{(\alpha,\mathrm{virt})}_{\mathrm{non-fact},u\bar{d}\to\nu_l l^+}$$

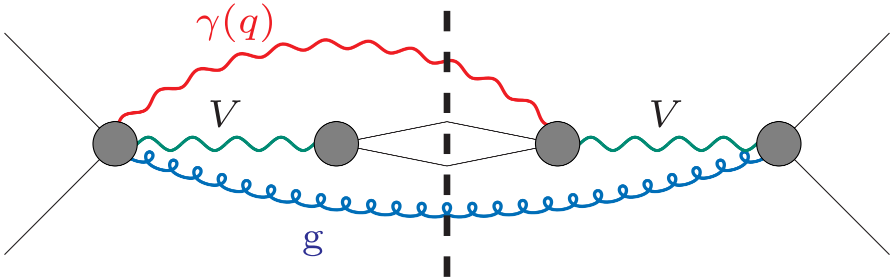
Real–virtual and real–real contributions to non-factorizable $\mathcal{O}(\alpha\alpha_s)$ corrections

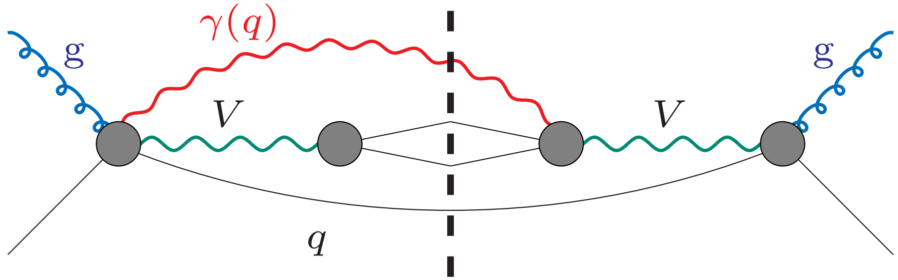




Result:

$$|\mathcal{M}|^2\Big|_{\substack{\mathrm{non-fact}\\ \mathrm{real-virt}}} = 2\,\mathrm{Re}\{\delta^{(\alpha_s,\mathrm{virt})}_{q\bar{q}'V}\}\,\delta^{(\alpha,\mathrm{real})}_{\mathrm{non-fact}}\,|\mathcal{M}_0|^2$$





Result:

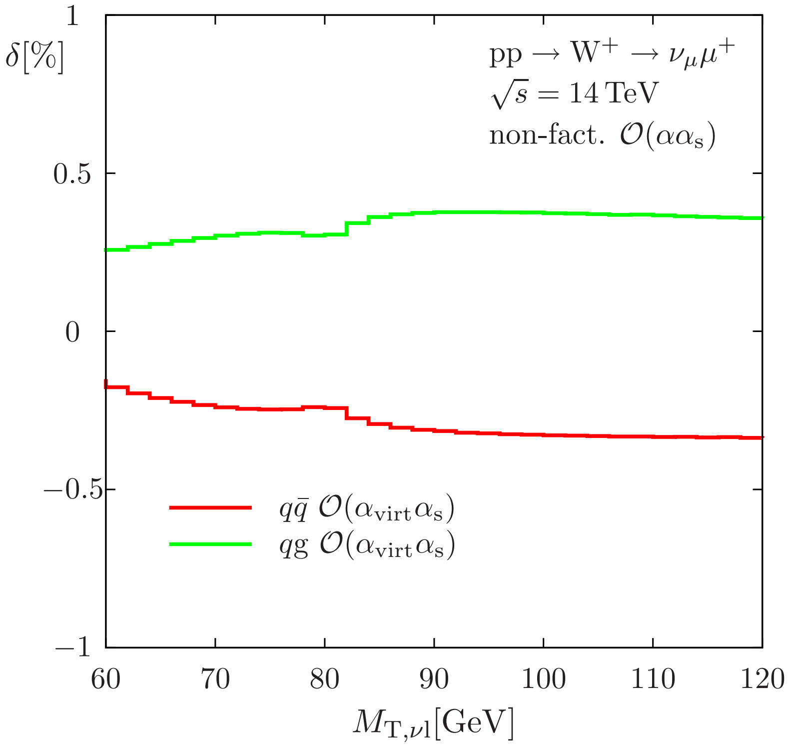
$$|\mathcal{M}|^2\Big|_{\substack{\mathrm{non-fact}\\ \mathrm{real-real}}} = \delta^{(\alpha,\mathrm{real})}_{\mathrm{non-fact}}\,|\mathcal{M}_{0,q\bar{q}\to l\bar{l}'\mathrm{g}}|^2, \qquad \text{etc.}$$

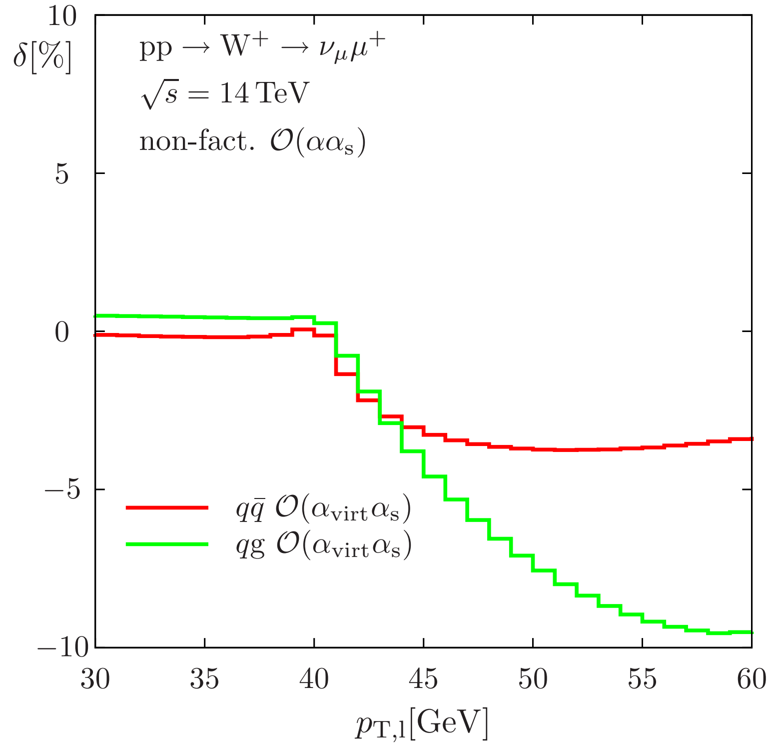
$$\delta^{(\alpha,\mathrm{real})}_{\mathrm{non-fact}} = \frac{\alpha}{2\pi^2}\int\frac{\mathrm{d}^3\mathbf{q}}{q^0}\,\mathrm{Re}\{\mathcal{J}^\mu_{\mathrm{prod}}\mathcal{J}^*_{\mathrm{dec},\mu}\}$$

Note: factorization, e.g., justified by YFS argument as in virtual–virtual case

Virtual-photon + soft-photon non-factorizable $\mathcal{O}(\alpha\alpha_s)$ corrections

W production:

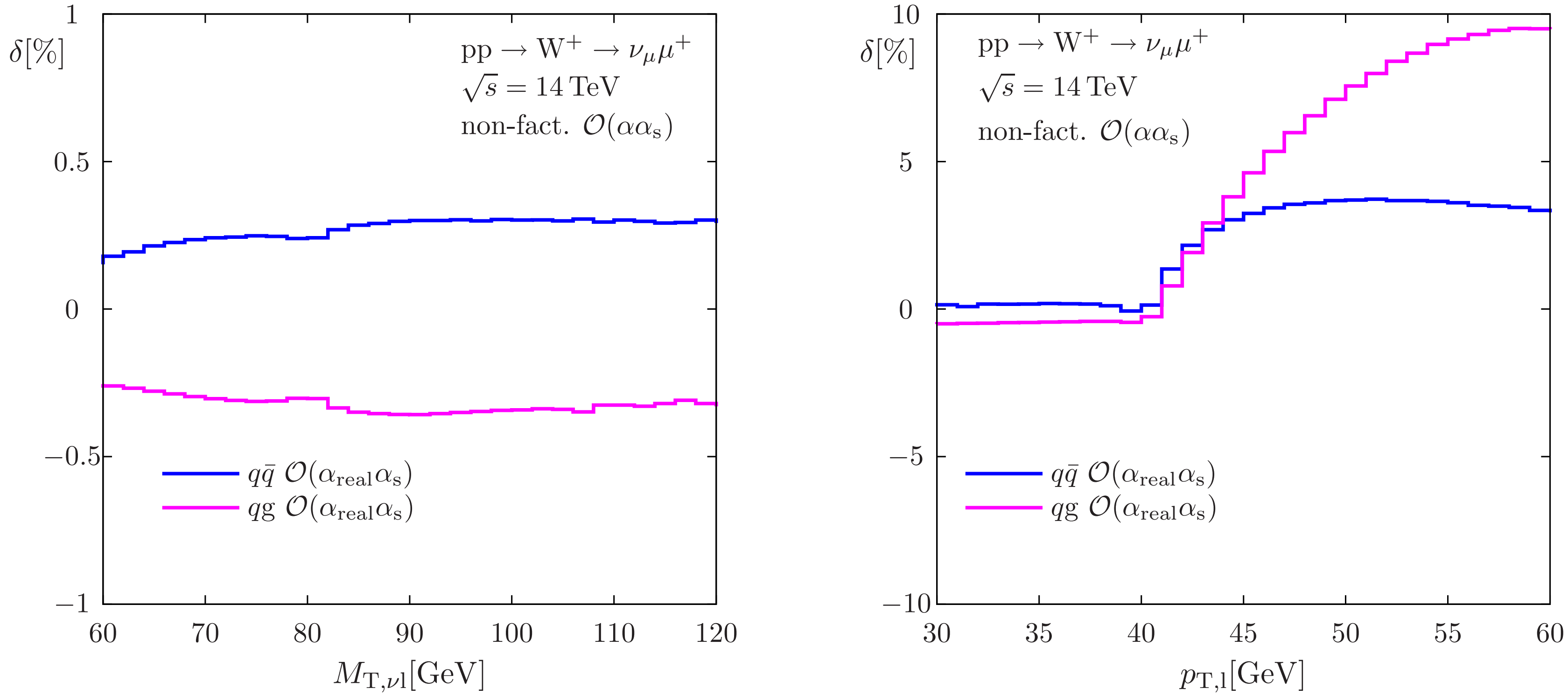




- $\delta \;=\; \delta_{\mathrm{non-fact,virt}\gamma} \;+\; \delta_{\mathrm{non-fact,soft}\gamma}(E_\gamma < \Delta E), \quad \Delta E = 10^{-4}\sqrt{\hat{s}}/2 \ll \Gamma_V$
- $M_{\mathrm{T},\nu l}$: corrections and distortion very small
- $p_{\mathrm{T},l}$: corrections several % with distortion
  $\hookrightarrow$ cancellation against real photonic corrections ??

Real-photon and full non-factorizable $\mathcal{O}(\alpha\alpha_s)$ corrections

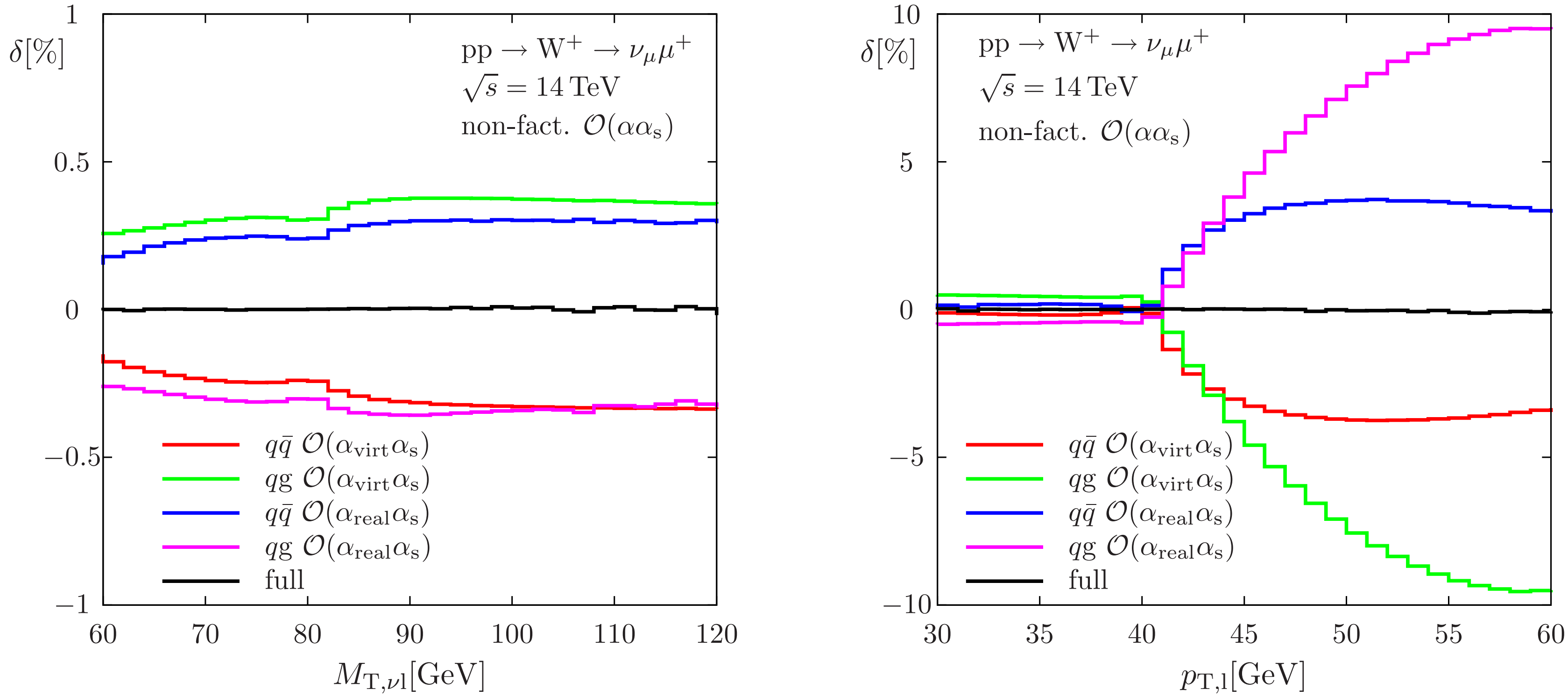
W production:



- $\delta \;=\; \delta_{\text{non-fact,real}\gamma}(E_\gamma > \Delta E), \quad \Delta E = 10^{-4}\sqrt{\hat{s}}/2 \ll \Gamma_V$

Real-photon and full non-factorizable $\mathcal{O}(\alpha\alpha_s)$ corrections

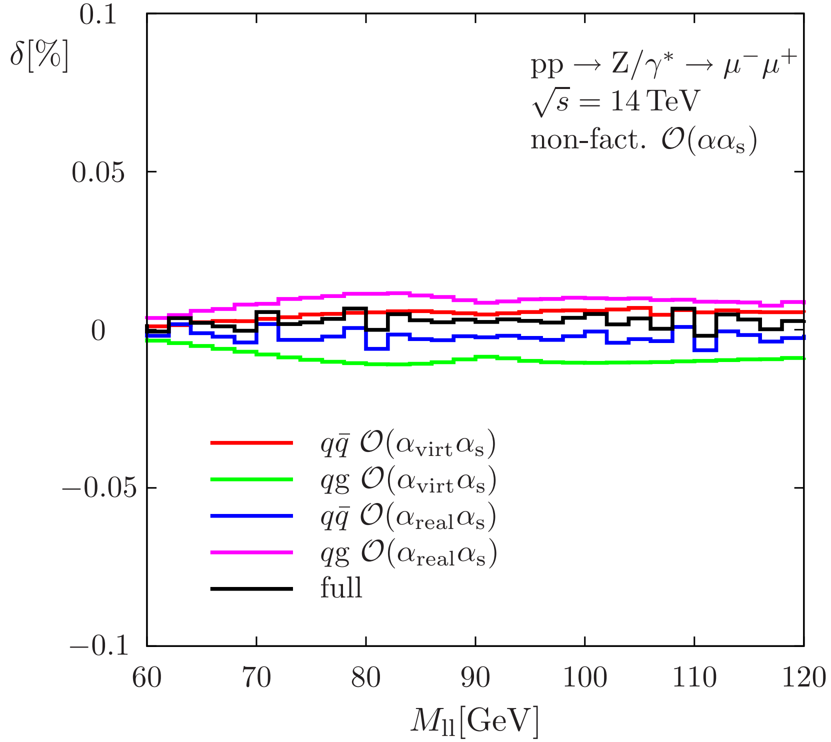
W production:

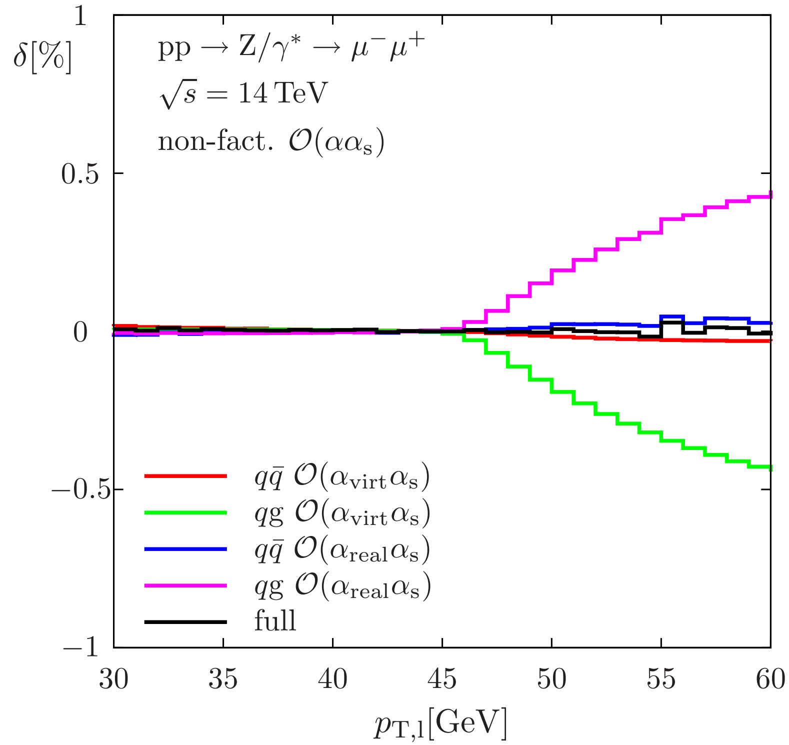


- $\delta \;=\; \delta_{\mathrm{non-fact,real}\gamma}(E_\gamma > \Delta E), \quad \Delta E = 10^{-4}\sqrt{\hat{s}}/2 \ll \Gamma_V$
- Full non-factorizable $\mathcal{O}(\alpha\alpha_s)$ corrections tiny
  due to complete cancellation between virtual and real corrections

Real-photon and full non-factorizable $\mathcal{O}(\alpha\alpha_s)$ corrections

Z production:

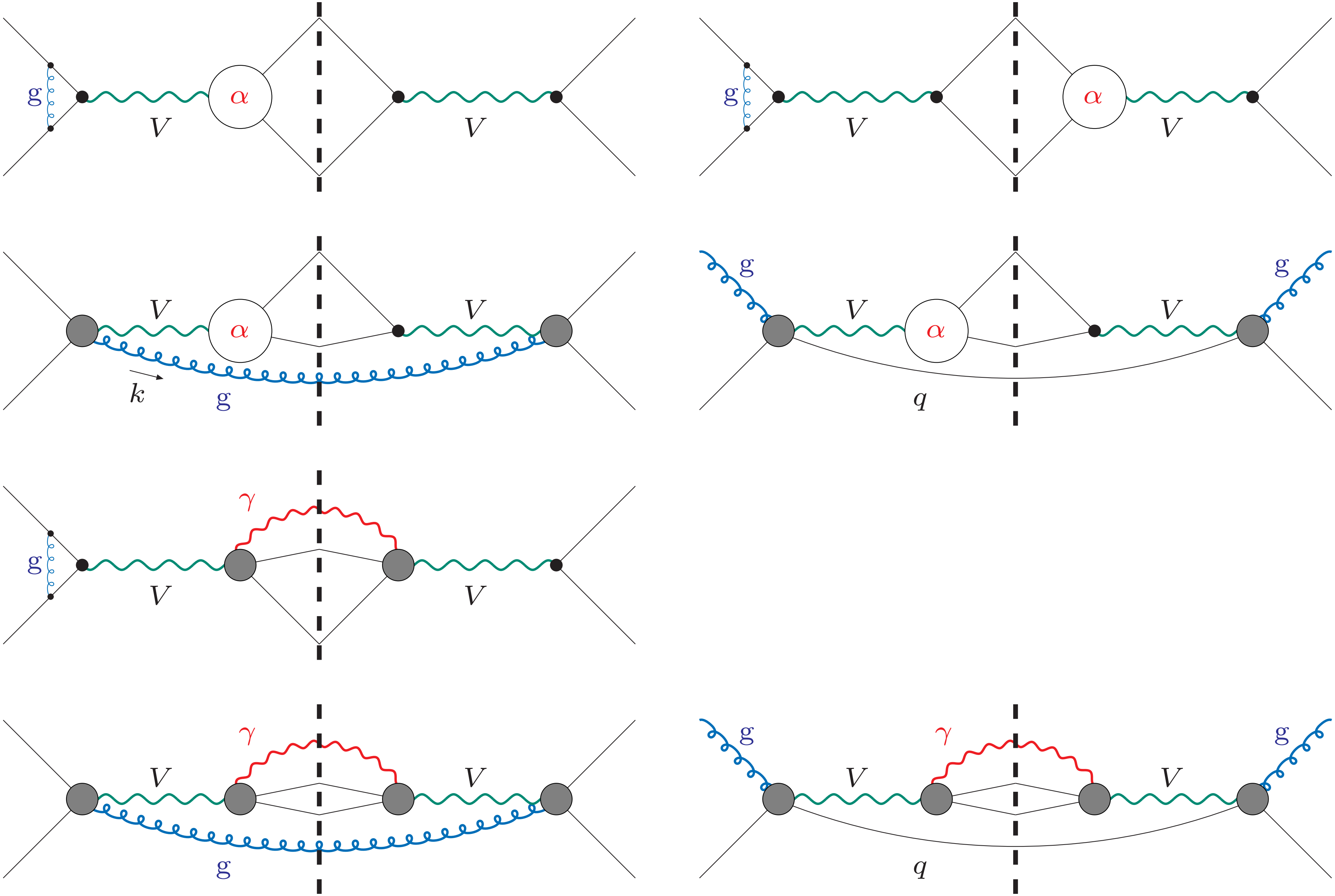




- $\delta \;=\; \delta_{\text{non-fact,real}\gamma}(E_\gamma > \Delta E), \quad \Delta E = 10^{-4}\sqrt{\hat{s}}/2 \ll \Gamma_V$
- Full non-factorizable $\mathcal{O}(\alpha\alpha_s)$ corrections tiny
  due to complete cancellation between virtual and real corrections

Dominant factorizable corrections

Contributions to initial–final factorizable $\mathcal{O}(\alpha\alpha_s)$ corrections



Full $\mathcal{O}(\alpha\alpha_s)$ corrections versus naive factorization

NLO QCD and EW corrections:

$$\sigma^{\mathrm{NLO_s}} \equiv \sigma^{\mathrm{LO}} \underbrace{(1+\delta_{\alpha_s})}_{=K^{\mathrm{NLO}}_{\mathrm{QCD}}} = \sigma^0 + \sigma^{\mathrm{LO}} \underbrace{\left(\frac{\sigma^{\mathrm{LO}}-\sigma^0}{\sigma^{\mathrm{LO}}} + \delta_{\alpha_s}\right)}_{\equiv \delta'_{\alpha_s}},$$

$$\Delta\sigma^{\mathrm{NLO_{ew}}} = \sigma^0\, \delta_\alpha, \qquad \sigma^0 = \text{LO contribution with NLO PDFs}$$

$\mathcal{O}(\alpha\alpha_s)$-corrected cross section:

$$\sigma^{\mathrm{NNLO_{s\otimes ew}}} = \sigma^{\mathrm{NLO_s}} + \Delta\sigma^{\mathrm{NLO_{ew}}} + \underbrace{\Delta\sigma^{\mathrm{NNLO_{s\otimes ew}}}_{\mathrm{ini-fin}}}_{=\sigma^{\mathrm{LO}}\,\delta^{\mathrm{ini-fin}}_{\alpha_s\alpha}}$$

Naive factorization @ $\mathcal{O}(\alpha\alpha_s)$:

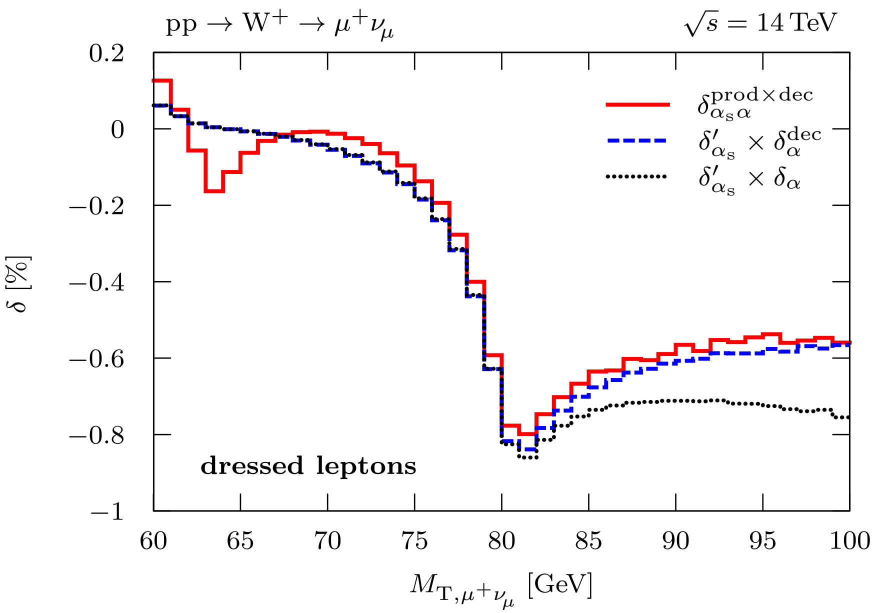
$$\sigma^{\mathrm{NNLO_{s\otimes ew}}}_{\mathrm{naive\,fact}} = \sigma^{\mathrm{NLO_s}}(1+\delta_\alpha) = \sigma^{\mathrm{LO}}(1+\delta_{\alpha_s})(1+\delta_\alpha)$$

$\Rightarrow$ Comparison of relative corrections:

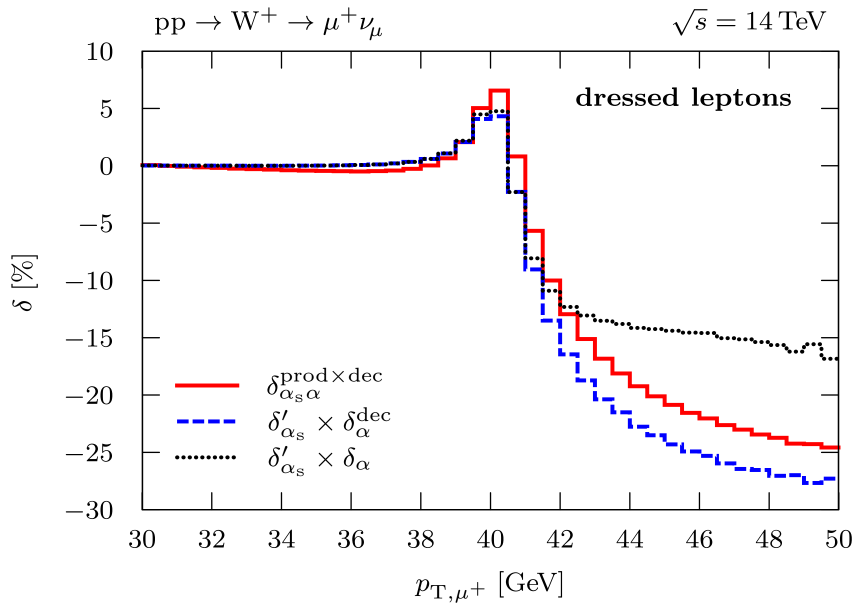
$$\frac{\sigma^{\mathrm{NNLO_{s\otimes ew}}} - \sigma^{\mathrm{NNLO_{s\otimes ew}}}_{\mathrm{naive\,fact}}}{\sigma^{\mathrm{LO}}} = \delta^{\mathrm{ini-fin}}_{\alpha_s\alpha} - \delta'_{\alpha_s}\delta_\alpha$$

Numerical results on initial–final factorizable $\mathcal{O}(\alpha\alpha_s)$ corrections

W production: (γ recombination applied, "dressed leptons")



Naive factorization works!



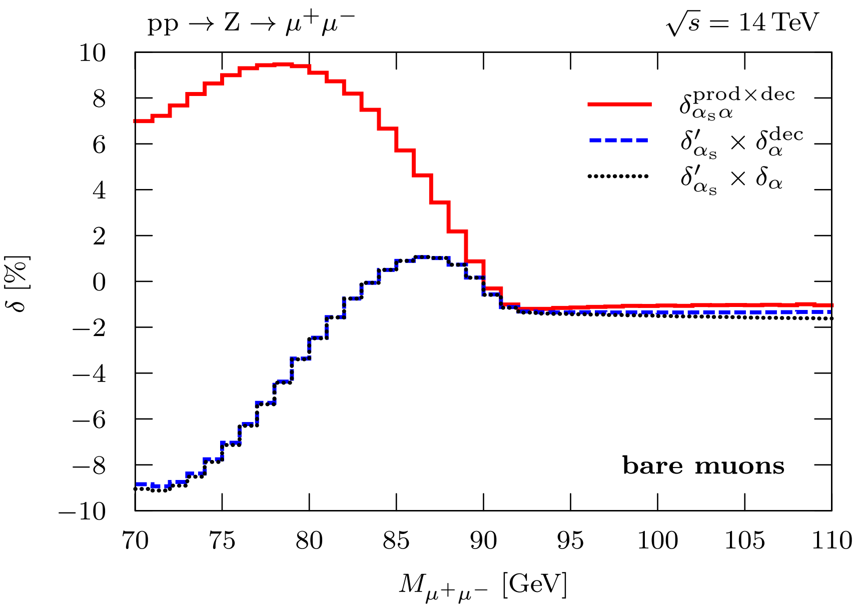
Naive factorization deteriorates for $p_{\mathrm{T},\mu^+} \gtrsim M_\mathrm{W}/2$

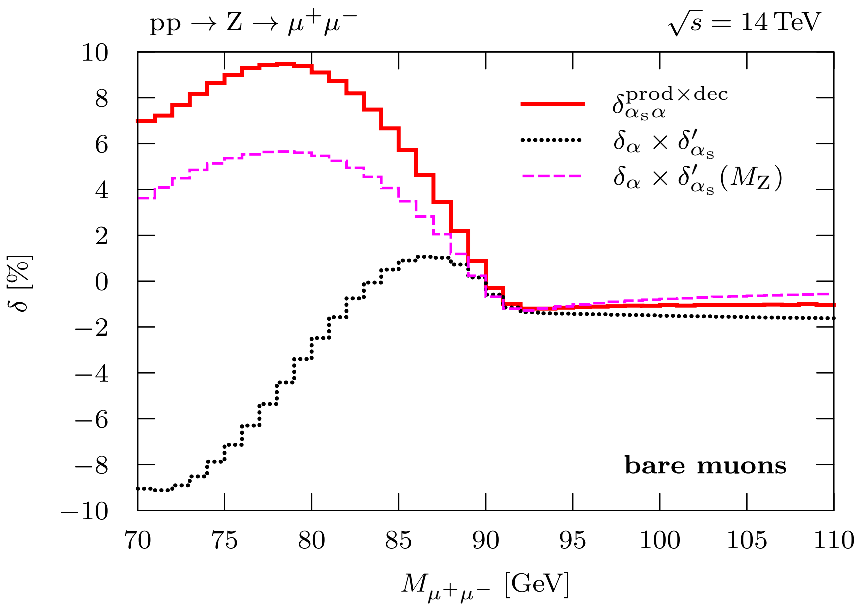
In progress:

- comparison of $\delta^{\mathrm{ini-fin}}_{\alpha_s\alpha}$ with MC approach $\mathrm{d}\sigma_{\alpha_s} \otimes$ (γ shower)
- estimate shifts in M_W by $\delta^{\mathrm{ini-fin}}_{\alpha_s\alpha}$

Numerical results on initial–final factorizable $\mathcal{O}(\alpha\alpha_s)$ corrections

Z production: (no γ recombination applied, "bare leptons")





Naive factorization fails !

Naive factorization takes "wrong QCD K factor"

In progress:

- comparison of $\delta_{\alpha_s\alpha}^{\mathrm{ini-fin}}$ with MC approach $\mathrm{d}\sigma_{\alpha_s} \otimes (\gamma$ shower)
- estimate shift in M_Z by $\delta_{\alpha_s\alpha}^{\mathrm{ini-fin}}$

Summary & outlook

High-precision Drell–Yan physics @ LHC

- promises M_W with accuracy $\Delta M_\mathrm{W} \lesssim 10\,\mathrm{MeV}$ and $\sin^2\theta_\mathrm{eff}^\mathrm{lept}$ with $\mathcal{O}$(LEP precision)
- requires highest possible theoretical precision near resonances
  NNLO QCD + NLO EW + QCD resummations etc. known
  $\mathcal{O}(\alpha\alpha_\mathrm{s})$ is biggest unknown correction

$\mathcal{O}(\alpha\alpha_\mathrm{s})$ in pole approximation

- non-factorizable corrections calculated $\to$ negligible
  $\hookrightarrow$ only factorizable corrections to $2 \to 1$ and/or $1 \to 2$ processes relevant
- $\mathcal{O}(\alpha\alpha_\mathrm{s})$ corrections to $q\bar{q}' \to V$ production
  $\hookrightarrow$ no significant resonance distortion expected
- $\mathcal{O}(\alpha\alpha_\mathrm{s})$ corrections to $V' \to l\bar{l}'$ decay
  $\hookrightarrow$ only irrelevant rescaling of distributions (only from counterterms)
- $\left[\mathcal{O}(\alpha_\mathrm{s}) \text{ to } q\bar{q}' \to V\right] \otimes \left[\mathcal{O}(\alpha) \text{ to } V' \to l\bar{l}'\right]$
  $\hookrightarrow$ significant resonance distortions expected, but straightforward to calculate

... paper in preparation, more details in Alexander Huss's talk

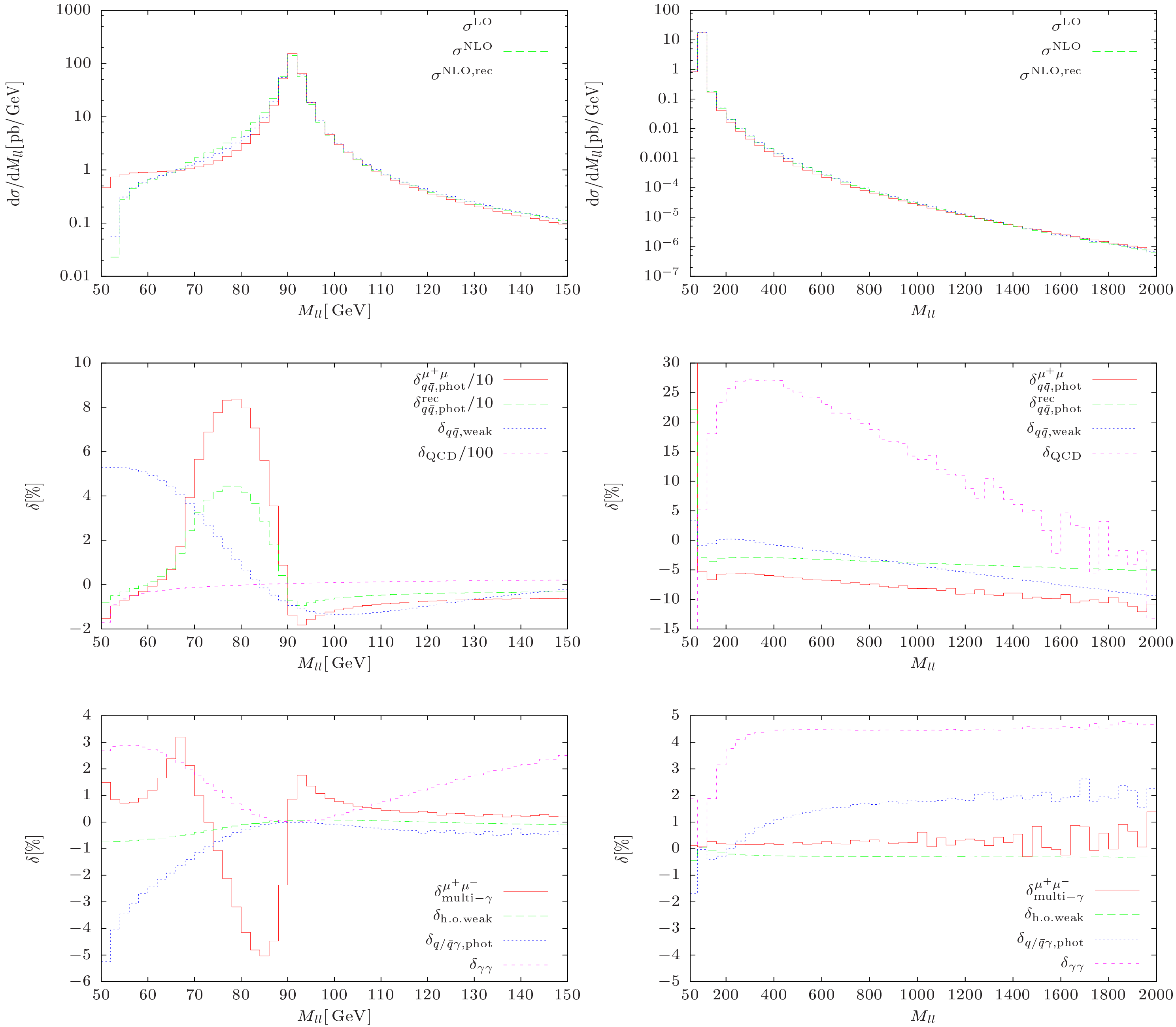
Backup slides

QCD and EW corrections to W/Z production:

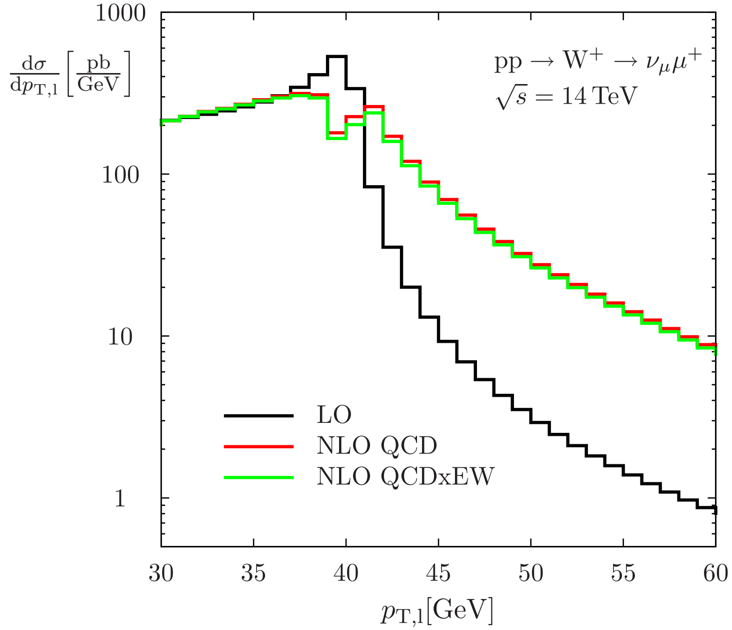
- NNLO QCD corrections
  Hamberg et al. ’91; Harlander, Kilgore ’02; Anastasiou et al. ’03; Melnikov, Petriello ’06; Catani et al. ’09
- soft + virtual N^{3}LO QCD
  Moch, Vogt ’05; Laenen, Magnea ’05; Idilbi et al. ’05; Ravindran, Smith ’07
- QCD resummations
  Arnold, Kauffman ’91; Balazs et al. ’95,’97; R.K.Ellis et al. ’97; Qiu, Zhang ’00; Kulesza et al. ’01,’02; Landry et al. ’02; Berge et al. ’05; Bozzi et al. ’08
- MC@NLO matching
  Frixione, Webber ’06
- NNLO PS matching
  Hoeche et al. ’14; Karlberg et al. ’14
- NLO EW correction to W production
  S.D., Krämer ’01; Zykunov ’01; Baur, Wackeroth ’04; Arbuzov et al. ’05; Carloni Calame et al. ’06; Brensing et al. ’07
- NLO EW correction to Z production
  Baur, Keller, Sakumoto ’97; Baur, Wackeroth ’99; Brein, Hollik, Schappacher ’99; Zykunov ’05; Arbuzov et al. ’06; Carloni Calame et al. ’07; S.D., Huber ’09
- multi-photon radiation via leading logs
  Baur, Stelzer ’99; Carloni Calame et al. ’03; Placzek, Jadach ’04; Brensing et al. ’07; S.D., Huber ’09
- photon-induced processes
  Arbuzov, Sadykov ’07; Brensing et al. ’07; Carloni Calame et al. ’07; S.D., Huber ’09
- POWHEG matching of QCD/EW corrs.
  Bernaciak, Wackeroth ’12; Barze et al. ’13
- NLO SUSY corrections in the MSSM
  Brensing et al. ’07; S.D., Huber ’09

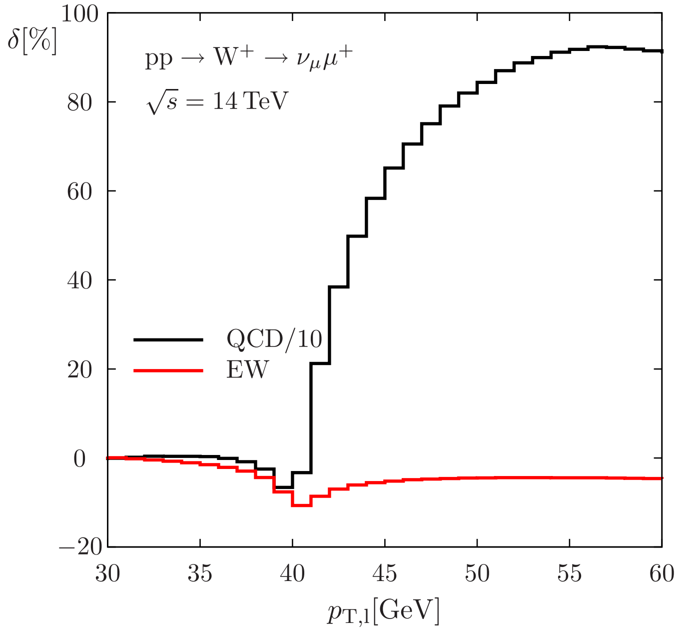
Corrections to Z production – overview

S.D., Huber '09



Transverse-momentum distribution for W production at NLO





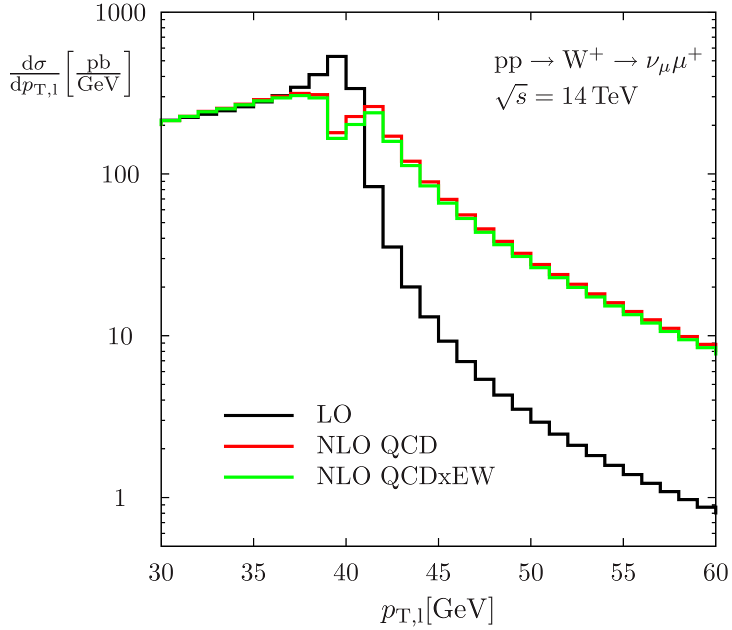
Features of $p_{T,l}$:

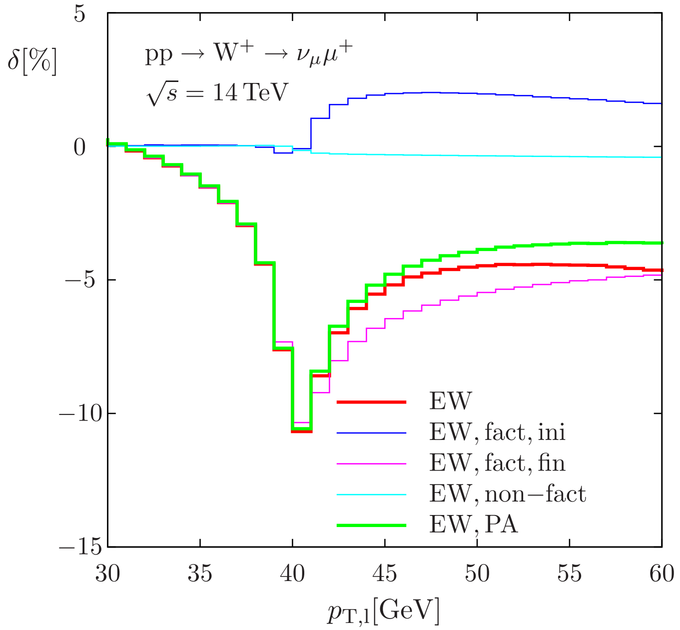
- also relevant for M_W measurement
- stability wrt detector effects
- sensitive to QCD effects/modelling/uncertainties

Corrections:

- QCD corrections huge above resonance (jet recoil)
- EW corrections distort resonance shape as well

Transverse-momentum distribution for W production at NLO





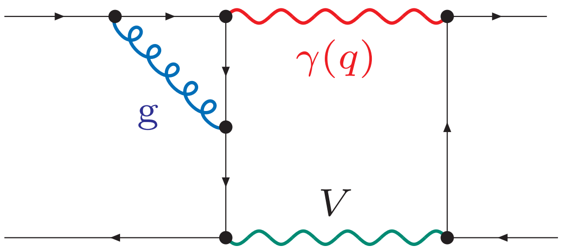
Features of $p_{\mathrm{T},l}$:

- also relevant for M_{W} measurement
- stability wrt detector effects
- sensitive to QCD effects/modelling/uncertainties

PA works well:

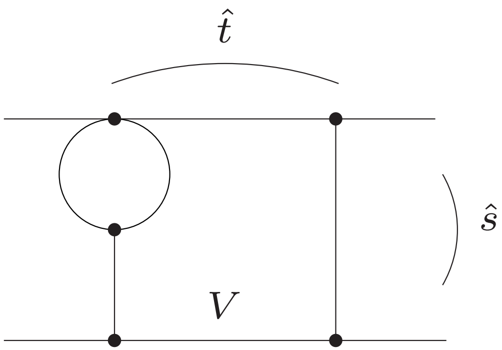
- EW corr reproduced near resonance
- factorizable FS corrs distort resonance shape
- factorizable IS corrs overwhelmed by QCD
- non-fact. corrs flat and negligible

Example: Two-loop box graph



$$\sim \quad -\frac{C_\mathrm{F}\alpha_\mathrm{s}}{4\pi}\,\frac{Q_q Q_l \alpha}{2\pi}\,\mathcal{M}_0\,(1-\epsilon)\,(-\hat{t})\,(\mu_V^2-\hat{s})\,I(\hat{s},\hat{t})$$

Master integral:



$$= \quad I(\hat{s},\hat{t}) \quad = \left(\frac{(2\pi\mu)^{2\epsilon}}{\mathrm{i}\pi^2}\right)^2 \int \mathrm{d}^D q \int \mathrm{d}^D q'\,\frac{1}{q^2\cdots}$$

$$\begin{aligned}
= \frac{c_\epsilon^2}{(-\hat{t})(\mu_V^2-\hat{s})}\left(\frac{\mu_V^2-\hat{s}}{M_V^2}\right)^{-3\epsilon}\left(\frac{-\hat{t}}{\mu^2}\right)^{-2\epsilon}\Bigg\{\frac{1}{2\epsilon^3}+\frac{1}{\epsilon^2}+\frac{1}{\epsilon}\left[\mathrm{Li}_2\left(1+\frac{\hat{t}}{M_V^2}\right)+\frac{5\pi^2}{12}+2\right] \\
+2\,\mathrm{Li}_3\left(\frac{-\hat{t}}{M_V^2}\right)+\mathrm{Li}_3\left(1+\frac{\hat{t}}{M_V^2}\right)-6\zeta(3)+\ln^2\left(\frac{-\hat{t}}{M_V^2}\right)\ln\left(1+\frac{\hat{t}}{M_V^2}\right) \\
-2\ln\left(\frac{-\hat{t}}{M_V^2}\right)\left[\frac{\pi^2}{6}-\mathrm{Li}_2\left(1+\frac{\hat{t}}{M_V^2}\right)\right]+\frac{5\pi^2}{6}+2\,\mathrm{Li}_2\left(1+\frac{\hat{t}}{M_V^2}\right)+4+\mathcal{O}(\hat{s}-\mu_V^2)+\mathcal{O}(\epsilon)\Bigg\}
\end{aligned}$$

Note: many cancellations in sum over all contributions $(1/\epsilon^4, \mathrm{Li}_3, \zeta(3), \ldots)$